## Unit 5: Thermodynamics, Radiation, Oscillations and Cosmology - Mark scheme

Question number	Answer	Mark
1	В	1
2	D	1
3	В	1
4	С	1
5	D	1
6	С	1
7	D	1
8	A	1
9	D	1
10	В	1

Question number	Answer	Mark
11	<ul> <li>The star is viewed from two positions at 6-month intervals         Or The star is viewed from opposite ends of the Earth's orbit diameter about the Sun</li></ul>	3
	Full marks may be obtained from a suitably annotated diagram, e.g. $E_{2}$ $R = 1 \text{A.U.}$ $E_{1}$ $E_{1}$ $Trigonometry is used to calculate d$	
	[Accept the symmetrical diagram seen in many textbooks]	
	Total for Question 11	3

Question	Answer		Mark
number			
12(a)	• Use of $\Delta E = mc\Delta\theta$	(1)	3
	• Use of $P = \frac{\Delta W}{\Delta t}$	(1)	
	• Time taken = $130 \text{ s}$	(1)	
	Example of calculation		
	$\Delta E = 3 \times 0.325 \text{ kg} \times 4190 \text{ J kg}^{-1} \text{ K}^{-1} \times (100 - 8.5) \text{K} = 373 800 \text{ J}$		
	$\Delta t = \frac{373\ 800\ J}{2.80 \times 10^3 W} = 134\ s$		
12(b)	• Use of $\Delta E = L\Delta m$	(1)	3
	Difference between power input and useful power calculated	(1)	
	• Rate of thermal energy transfer to surroundings = 340 W	(1)	
	Example of calculation		
	$\frac{\Delta E}{\Delta t} = 2.26 \times 10^6 \text{ J kg}^{-1} \times \frac{0.136 \text{ kg}}{125 \text{ s}} = 2460 \text{ W}$		
	Rate of thermal energy transfer to surroundings = $2800 \text{ W} - 2460 \text{ W} = 340 \text{ W}$		
	Total for Question 12		6

Question number	Answer	Mark
13(a)	• $\alpha \operatorname{correct}(1)$ (1) • Th correct (1) (1)	2
13(b)(i)	• Use of $A = -\lambda N$ • Use of $\lambda = \frac{\ln 2}{t_{1/2}}$ • $N = 7.47 \times 10^{18}$ (1) • $N = \frac{\ln 2}{1.41 \times 10^{17} \text{s}} = 4.91 \times 10^{-18} \text{s}^{-1}$ $36.7 \text{ s}^{-1} = -4.91 \times 10^{-18} \text{s}^{-1} \times N$ $\therefore N = \frac{36.7 \text{ s}^{-1}}{4.91 \times 10^{-18} \text{s}^{-1}} = 7.47 \times 10^{18}$	3

Question number	Answer	Mark
13(b)(ii)	• The decay products are radioactive  Or the background radiation should be subtracted from the recorded count rate  (1)	1
	Total for Question 13	6

Question number	Answer		Mark
14(a)	<ul> <li>Conversion of temperature from °C to K</li> <li>N = 3.82 × 10<sup>23</sup></li> </ul>	(1) (1) (1)	3
	$N = \frac{1.10 \times 10^5 \text{Pa} \times 0.0142 \text{ m}^3}{1.38 \times 10^{-23} \text{J K}^{-1} \times (23.5 + 273) \text{K}} = 3.82 \times 10^{23}$		
14(b)	• (so the volume of the balloon will increase) until the pressure exerted by	(1) (1)	2
	Total for Question 14		5

Question number	Answer	Mark
15(a)	The binding energy is:	1
	• The energy released when the nucleons come together to form the nucleus <b>Or</b> The energy required to split the nucleus up into its component nucleons (1)	)
15(b)(i)	• Calculation of mass difference in kg • Use of $\Delta E = c^2 \Delta m$ (1) • Conversion from kg into MeV • $\Delta E = 8.5 \text{ MeV}$	)
	Example of calculation $\Delta m = (1.00728 + [2 \times 1.00867] - 3.01551)u \times 1.66 \times 10^{-27} \text{kg}$ $\therefore \Delta m = 1.51 \times 10^{-29} \text{ kg}$ $\Delta E = (3 \times 10^8 \text{m s}^{-1})^2 \times 1.51 \times 10^{-29} \text{kg} = 1.36 \times 10^{-12} \text{J}$ $\Delta E = \frac{1.36 \times 10^{-12} \text{J}}{1.6 \times 10^{-13} \text{J MeV}^{-1}} = 8.49 \text{ MeV}$	
15(b)(ii)	When massive nuclei undergo fusion the binding energy per nucleon decreases     Hence energy must be supplied in order for fusion to proceed	)
	Total for Question 15	7

Question number	Answer		Mark
16(a)	• Use of $L = 4\pi r^2 \sigma T^4$	(1)	2
	• $r = 6.9 \times 10^8 \text{ m}$ Example of calculation $r = \sqrt{\frac{3.85 \times 10^{26} \text{W}}{4\pi \times 5.67 \times 10^{-8} \text{W m}^{-2} \text{ K}^{-4} \times (5800)^4}} = 6.91 \times 10^8 \text{m}$	(1)	
16(b)	• Use of $I = \frac{L}{4\pi d^2}$ • Use of fraction dissipated • Use of efficiency= $\frac{\text{useful power out}}{\text{total power input}}$ • Use of $I = \frac{P}{A}$ • $P = 56 \text{ MW}$ Example of calculation $I = \frac{3.85 \times 10^{26} \text{W}}{4\pi \times (1.50 \times 10^{11} \text{m})^2} = 1360 \text{ W m}^{-2}$ $P = 1360 \text{ W m}^{-2} \times (1-0.25) \times 0.22 \times 250 000 \text{ m}^2 = 5.61 \times 10^7 \text{ W}$	(1) (1) (1) (1) (1)	5
	Total for Question 16		7

Question number	Answer		Mark
17(a)	Resonance	(1)	1
17(b)	• Use of $f = \frac{n}{t}$ • Use of $\omega = 2\pi f$ • Use of $a = -\omega^2 x$ • $a = 14 \text{ m s}^{-2}$ Example of calculation $f = \frac{38}{60 \text{ s}} = 0.633 \text{ s}^{-1}$ $\omega = 2\pi \times 0.633 \text{ s}^{-1} = 3.98 \text{ rad s}^{-1}$ $\alpha = -(3.98 \text{ rad s}^{-1})^2 \times 0.90 \text{ m} = 14.3 \text{ m s}^{-2}$	(1) (1) (1) (1)	4
17(c)(i)	Both forces drawn and labelled  Example of diagram  (normal) reaction/R  weight/mg/W	(1)	1
17(c)(ii)	<ul> <li>There must always be an acceleration towards the equilibrium position</li> <li>Or there must always be a resultant force towards the equilibrium position</li> <li>(Applying Newton's 2<sup>nd</sup> law) W − R = ma so R = W − ma</li> <li>If a ≥ g, then R = 0 and so car will lose contact with the road</li> </ul>	(1) (1) (1)	3
	Total for Question 17		9

18(a) 18(b)	<ul> <li>The fan in the toy pushes the air r</li> <li>According to Newton's 3rd law, t molecules</li> </ul>		(1)	3
	• According to Newton's 3rd law, t			
18(b)			(1)	
18(b)		The state of the s		
18(b)	• The upward force balances the we	eight of the toy	(1)	
	This question assesses a student's abi			6
	structured answer with linkages and f	ully-sustained reasoning.  tent and for how the answer is structured		
	and shows lines of reasoning.	tent and for now the answer is structured		
		arks should be awarded for indicative		
	content.			
	Number of Number of marks			
	indicative awarded for			
	marking points indicative seen in answer marking points			
	6 4			
	5–4 3			
	3–2 2			
	1 1			
	The following table shows how the mand lines of reasoning.	larks should be awarded for structure		
	The state of reasoning.	Number of marks awarded for	1	
		structure of answer and sustained		
		line of reasoning		
	Answer shows a coherent and	2		
	logical structure with linkages and fully sustained lines of			
	reasoning demonstrated			
	throughout			
	Answer is partially structured	1		
	with some linkages and lines of			
	reasoning			
	Answer has no linkages	0		
	between points and is	U		
	unstructured			
			<u> </u>	
	Total marks awarded is the sum of m			
	marks for structure and lines of reaso	ning		
	Indicative content			
	• applying Newton's 3rd law, toy A	A exerts a force on toy B and vice versa		
	• forces equal in magnitude and op	posite in direction		
	• forces act for same time			
	• $F\Delta t_{\rm A} = -F\Delta t_{\rm B}$			
	• applying Newton's 2nd law $F\Delta t$	$=\Delta p$		
	• total momentum change = 0, so n Or $\Delta p$ for one toy = $-\Delta p$ for the	nomentum conserved other toy, so momentum is conserved		
	<b>Total for Question 18</b>			9

Question number	Answer		Mark
19(a)	For simple harmonic motion the acceleration of the tyre is:		2
	directly proportional to displacement from equilibrium position	(1)	
	<ul> <li>always acting towards the equilibrium position</li> <li>Or idea that acceleration is in the opposite direction to displacement</li> </ul>	(1)	
	[Accept definition in terms of force]		
19(b)(i)	• Use of $\omega = \frac{2\pi}{T}$ with $T = 3$ s	(1) (1)	3
	• Use of $a = -\omega^2 x$ • $A = 0.46 \text{ m}$	(1)	
	✓ A = 0.40 III		
	Example of calculation		
	$\omega = \frac{2\pi}{6.0 \text{ s/2}} = 2.09 \text{ rad s}^{-1}$		
	$A = \frac{2 \text{ m s}^{-2}}{(2.09 \text{ rad s}^{-1})^2} = 0.456 \text{ m}$		
19(b)(ii)	• Use of $v = A\omega \sin \omega t$	(1)	2
	• $v = 0.95 \text{ m s}^{-1}$ (allow e.c.f. $\omega$ and $A$ from b(i))	(1)	
	Example of calculation		
	$v = 0.456 \text{ m} \times 2.09 \text{ rad s}^{-1} = 0.953 \text{ m s}^{-1}$		

Question number	Answer	Mark
19(b)(iii)	<ul> <li>Sine curve drawn with correct shape and time period of 3 s</li> <li>Constant amplitude [any size] (MP2 dependent upon MP1)</li> </ul>	2
	Examples of graphs:	
	$a/m s^{-2}$ 2.0 0 -2.0	
	This graph has been carefully sketched, with construction lines and positions of maxima and minima marked before making the freehand graph sketch.	
	2.0 0 -2.0	
	This graph has been sketched without the aid of construction lines. Positions of maxima and minima have not been marked. The maxima are slightly displaced from their correct positions, although the shape is generally good and the amplitude is constant.	
	Total for Question 19	9

Question number	Answer		Mark
20(a)(i)	• States $F = \frac{GMm}{r^2}$	(1)	2
	• $mg = \frac{GMm}{r^2}$ leading to $g = \frac{GM}{r^2}$	(1)	
20(a)(ii)	• $g = \frac{GM}{r^2}$ combined with $a = r\omega^2$		4
	Or $F = \frac{GMm}{r^2}$ combined with $F = mr\omega^2$	(1)	
	(accept equations in terms of $v$ or $\omega$ )		
	• Use of $\omega = \frac{2\pi}{T}$ Or $v = \frac{2\pi r}{T}$	(1)	
	• Maths to show $T^2 = \frac{4\pi^2 r^3}{GM}$	(1)	
	• $\pi$ , G and M identified as being constant, so $T^2 \propto r^3$	(1)	
	Example of derivation		
	$\frac{GM}{r^2} = r\omega^2 = r\left(\frac{2\pi}{T}\right)^2$		
	$\therefore \frac{GM}{r^2} = \frac{4\pi^2 r}{T^2}$		
	, 1		
	$\therefore T^2 = \frac{4\pi^2 r^3}{GM}$		
	$\therefore T^2 \propto r^3$		
20(b)(i)	• $T = 24$ hours for a geostationary orbit	(1)	3
	• Use of $T^2 \propto r^3$ • $h = 3.5 \times 10^7 \text{ m}$	(1) (1)	
	Example of calculation		
	$\left  \frac{T_1^2}{T_2^2} = \frac{r_1^3}{r_2^3} \right $		
	$T_2^2 - \overline{r_2^3}$		
	$\therefore r_2 = \sqrt[3]{\frac{(24 \times 60 \text{ min})^2}{(88 \text{ min})^2}} \times 6.4 \times 10^6 \text{m} = 4.13 \times 10^7 \text{m}$		
	$h = 4.13 \times 10^7 \text{m} - 6.4 \times 10^6 \text{m} = 3.49 \times 10^7 \text{m}$		
20(b)(ii)	• Idea that there must be a common axis of rotation for the satellite and		1
	the Earth  Or the plane of the satellite's orbit must be at right angles to the spin		
	axis of the Earth	(1)	
	Total for Question 20		10

Question number	Answer		Mark
21(a)(i)	A main sequence star is fusing/burning hydrogen in its core	(1)	1
21(a)(i)	Diagonal region from top left to bottom right to include the Sun and Proxima Centauri	(1)	1
	Example of diagram  L/L <sub>Sun</sub> 10 <sup>6</sup> 10 <sup>4</sup> 10 <sup>2</sup> 1 +Sirius B +Proxima Centauri 24000 12000 6000 3000 T/K		
21(b)(i)	<ul> <li>Alpha Orionis and Proxima Centauri both have a surface temperature of about 3000 K</li> <li>So according to Wien's law (λ<sub>max</sub>T = 2.9 × 10<sup>-3</sup>) both will emit emradiation that peaks in the same region of the spectrum</li> <li>Alpha Orionis has a much greater luminosity than Proxima Centauri</li> <li>According to Stefan's law (L = 4πr²σT⁴) so Alpha Orionis must have a much larger radius than Proxima Centauri hence the statement is not valid</li> </ul>	(1) (1) (1)	4
21(b)(ii)	<ul> <li>Sirius B is off the main sequence, has a much higher surface temperature but about the same luminosity as Proxima Centauri</li> <li>So hydrogen fusion has ceased in the core of Sirius B whereas it hasn't for Proxima Centauri</li> <li>Since Sirius B is much hotter but about the same luminosity this means it must have a much smaller radius than Proxima Centauri</li> </ul>	(1) (1) (1)	3
	Total for Question 21		9